Bottomonium suppression in the quark-gluon plasma

Michael Strickland

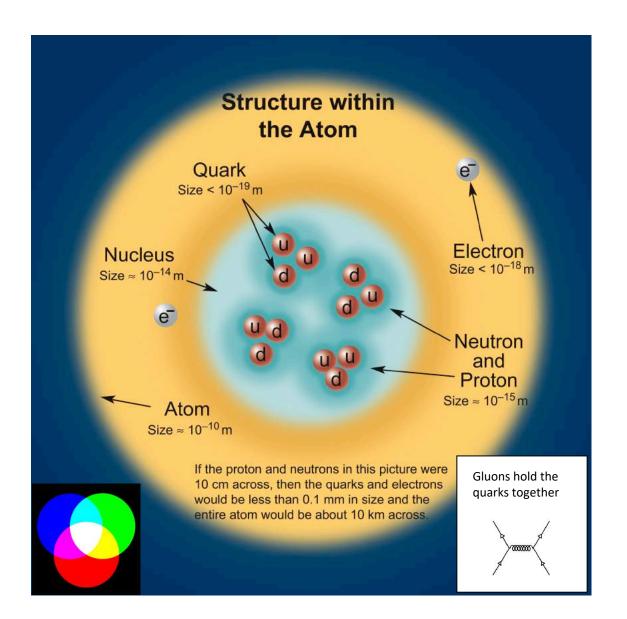
Kent State University Kent, OH USA

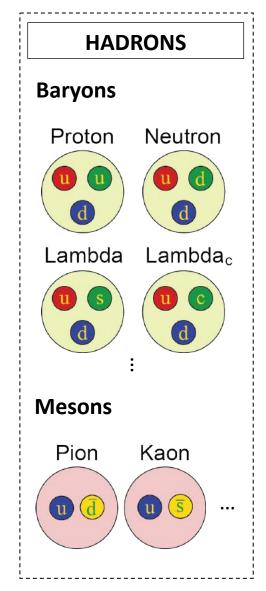
Sharif University of Technology July 14, 2020





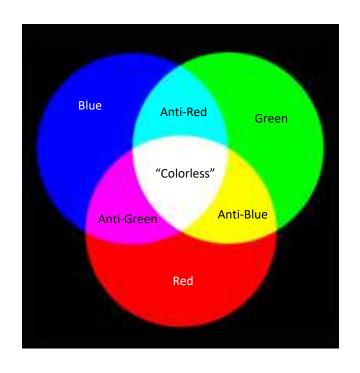
Quarks are normally "confined" inside hadrons

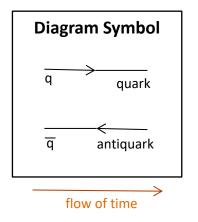




Quarks and anti-quarks

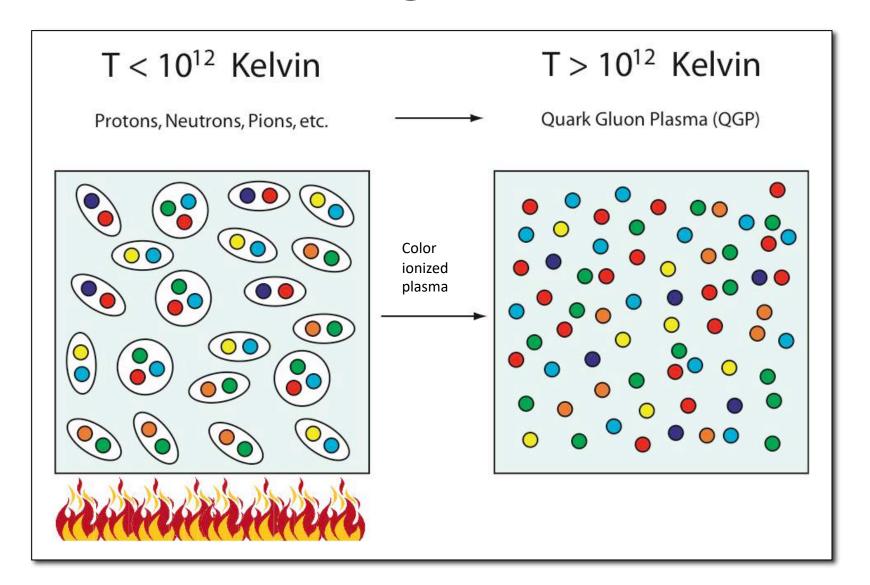
Name		Mass [GeV/c²]	Electric Charge
Up	u	0.0024	+2/3
Down	d	0.0048	-1/3
Strange	S	0.104	-1/3
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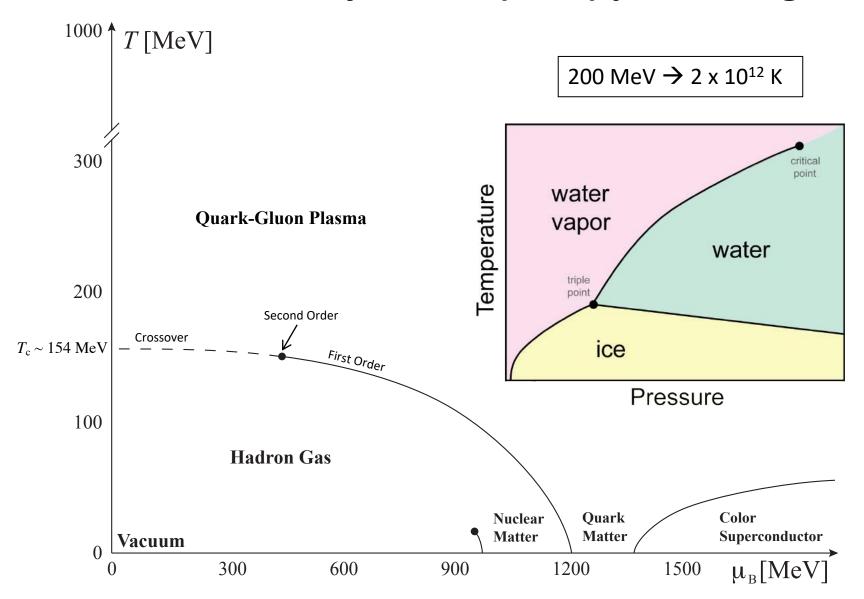


- Quarks are fermions (spin ½);
 have electric charge and "color charge"
- There are also anti-quarks that have the opposite electric charge and "anti-color charge"
- The proton is (primarily) composed of uud
- Compare the masses above to the mass of the proton which is ~ 1 GeV

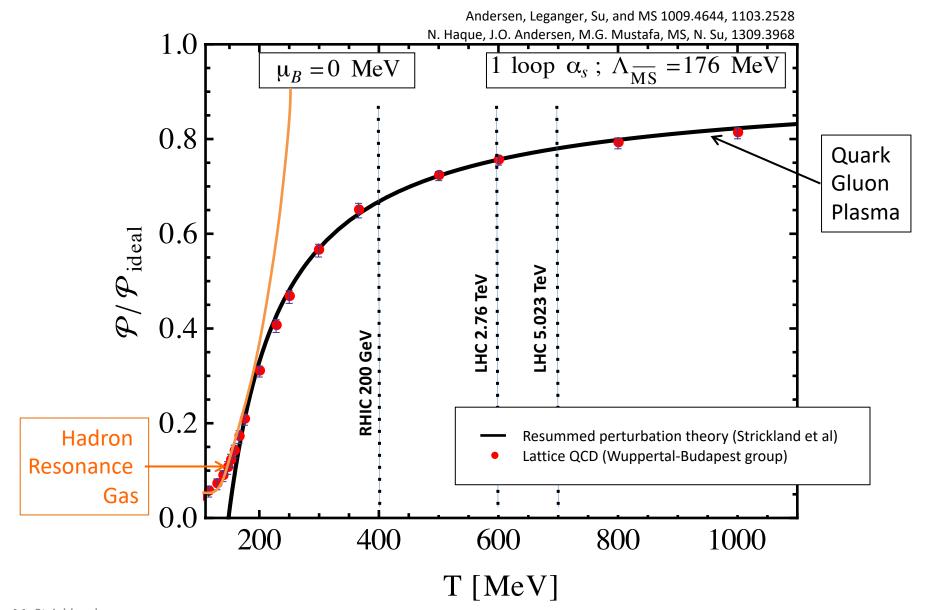
Melting hadrons



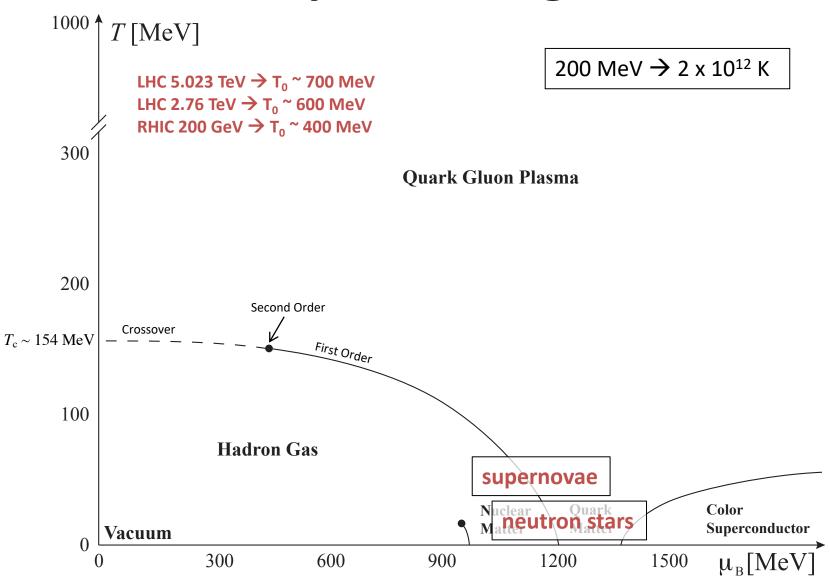
Quantum chromodynamics (QCD) phase diagram



Pressure vs temperature – μ_B = 0 MeV

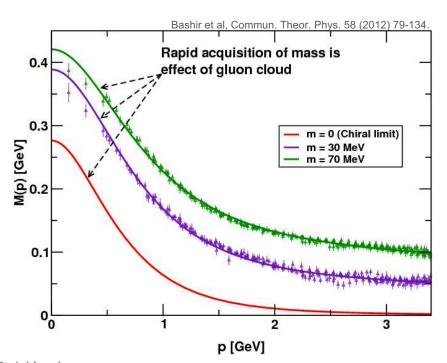


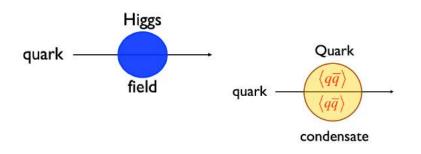
QCD phase diagram

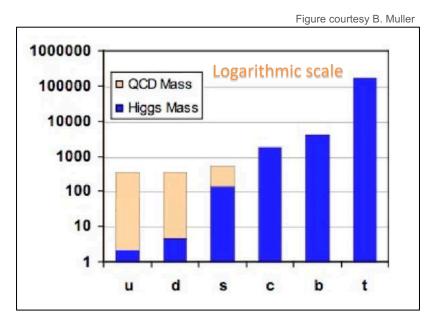


98% of the mass in the universe is made during the QGP transition

- The Higgs boson only provides a small fraction of the mass of observed hadronic matter.
- Most of the mass around us emerges from the strong force.



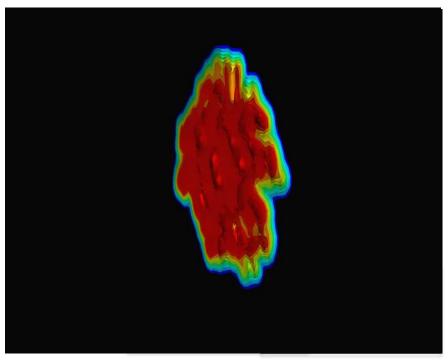


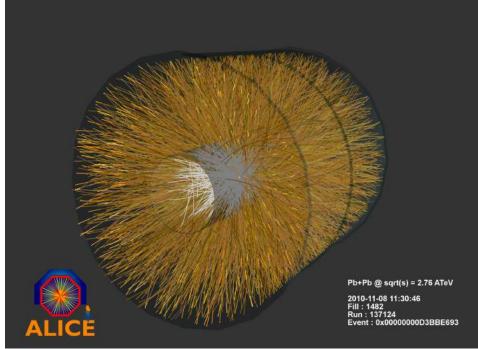


Experiments and Phenomenology

Ultrarelativistic heavy-ion collisions

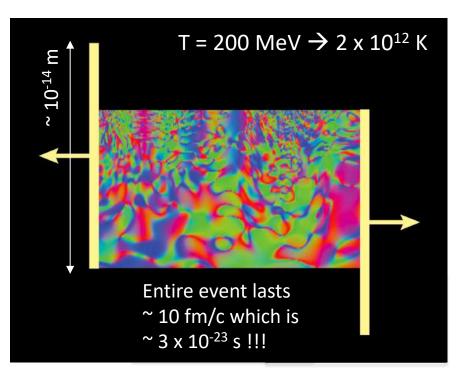
- RHIC, BNL Au-Au @ 200 GeV/nucleon (highest energy) \rightarrow T₀ ~ 400 MeV
- **LHC**, CERN Pb-Pb @ 2.76 TeV \rightarrow T₀ ~ 600 MeV
- **LHC**, CERN Pb-Pb @ 5.03 TeV \rightarrow T₀ ~ 700 MeV
- RHIC, BNL BES Au-Au @ 7.7 39 GeV \rightarrow T₀ ~ 30-100 MeV [+finite density]
- FAIR (GSI), NICA (Dubna) U-U @ 35 GeV -> $T_0 \sim 100$ MeV [+finite density]

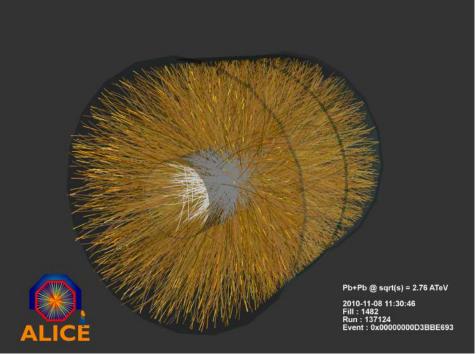




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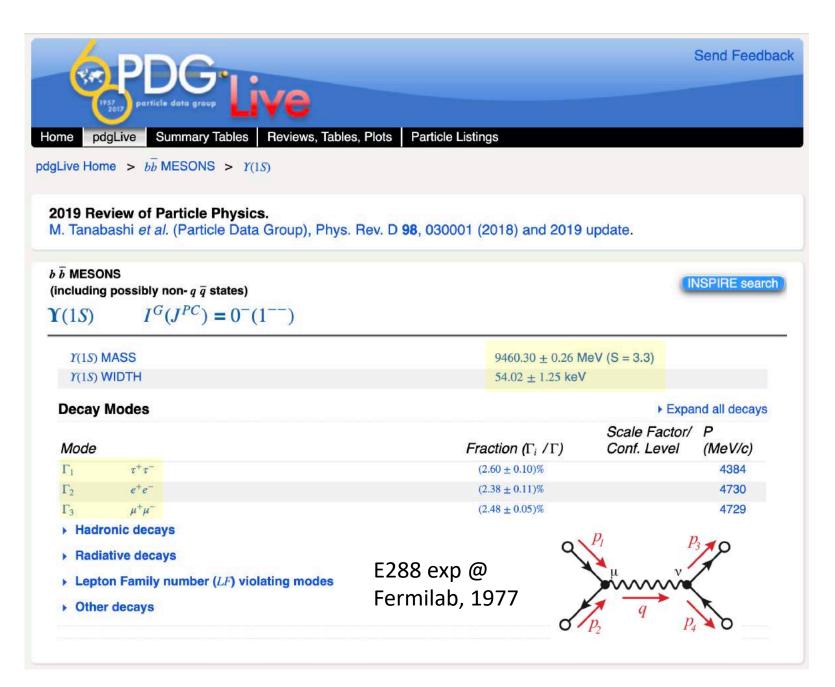
Some Key Experimental Observables

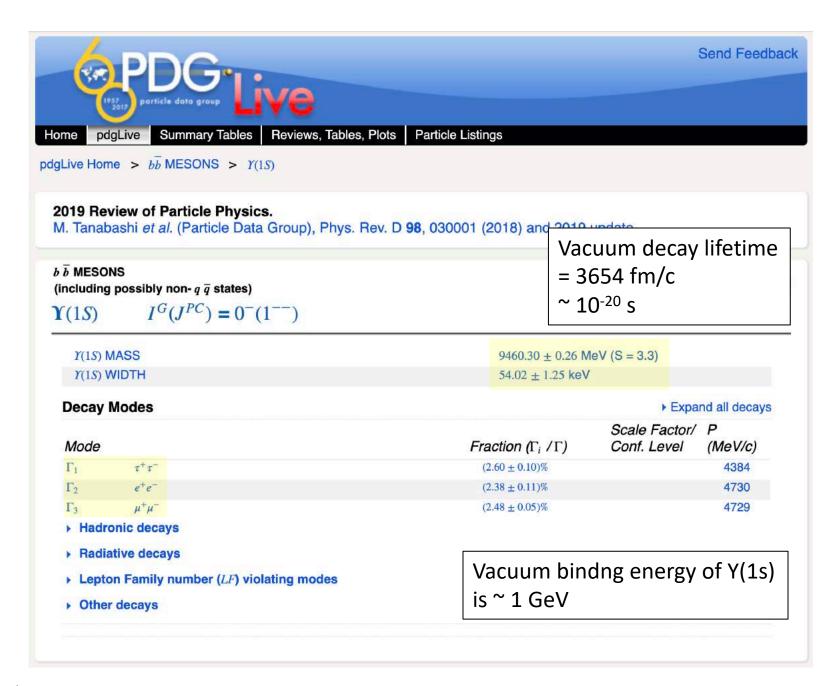
- Collective Flow flow of the matter provides evidence of collectivity in the QGP and allows us to extract transport coefficients like the shear viscosity
- Jet Quenching effects of plasma interactions on high-energy particle propagation; provides information about momentum diffusion and energy loss of partons in the QGP
- Suppression of heavy quarkonia provides information about screening and bound state survival in the QGP
- **Electromagnetic Radiation** high energy photons and dileptons provide information about initial conditions
- Particle spectra across species provides information about the degree to which final particle distributions are thermalized
- Multiparticle correlations such as Hanbury-Brown-Twiss (HBT) interferometry –
 provides information about the size of the QGP and collective flow profiles

Some Key Experimental Observables

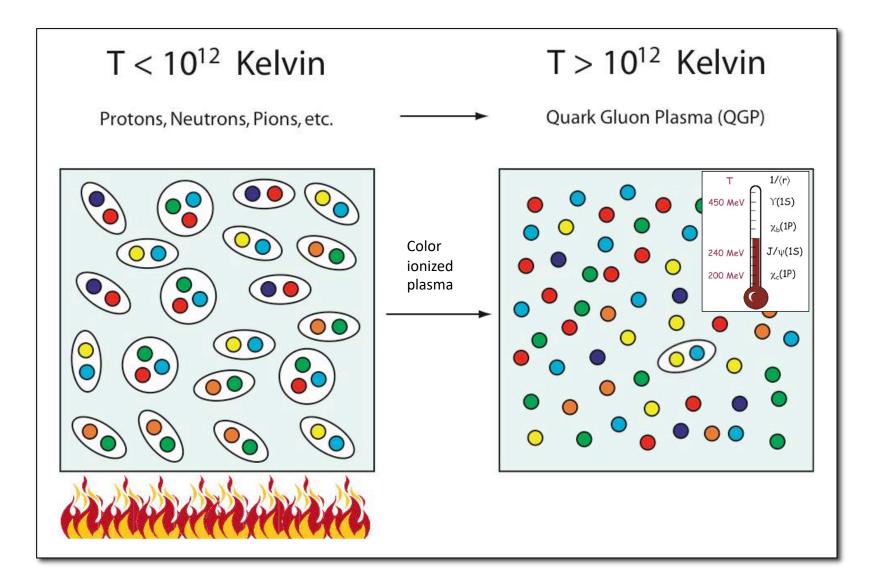
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Why heavy quarkonia?



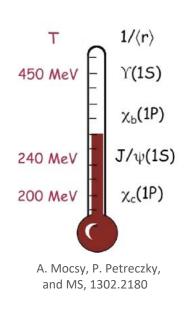


Melting hadrons - conceptual correction



Why bottomonia in AA?

- Can reliably use heavy quark effective theory
- Cold nuclear matter (CNM) effects in AA decrease with increasing quark mass
- The masses of bottomonia (~ 10 GeV) are much higher than the temperature (T < 1 GeV) generated in HICs → bottomonia production dominated by initial hard scatterings



 Since bottom quarks and anti-quarks are relatively rare in LHC HICs, the probability for regeneration of bottomonia through statistical recombination is much smaller than for charm quarks [see e.g. E. Emerick, X. Zhao, and R. Rapp, arXiv:1111.6537]

Heavy quark effective theory

Name		Mass [GeV/c²]	Electric Charge
Up	u	0.0024	+2/3
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- Normally, for QCD bound states one needs a fully relativistic treatment
- If the quark mass is sufficiently high then one can take the "heavy quark limit"
- This reduces the problem to having to deal with a nonrelativistic terms plus relativistic corrections

$$H = \frac{1}{2m} \left(\vec{p}_{\varphi} - q \vec{A}_{\varphi}^{QED} \right)^{2} + \frac{1}{2m} \left(\vec{p}_{\chi} + q \vec{A}_{\chi}^{QED} \right)^{2} - \frac{4\alpha_{s}}{3} \frac{1}{r} + \sigma r - \frac{q}{2m} \left(\vec{\sigma}_{\varphi} + \vec{\sigma}_{\chi} \right) \cdot \vec{B}_{background} - \frac{\alpha_{s}}{3m^{2}} \frac{1}{r^{3}} - \frac{1}{2m^{2}} \left(\frac{\alpha_{s}}{3} \frac{1}{r^{3}} + \frac{\sigma}{4} \frac{1}{r} \right) \left(\vec{\sigma}_{\varphi} \cdot \vec{r} \times \vec{p}_{\varphi} - \vec{\sigma}_{\chi} \cdot \vec{r} \times \vec{p}_{\chi} \right) + 2m ,$$
(90)

How well does this work?

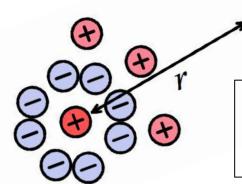
State	Name	Exp. [92]	Model	Rel. Err.
1^1S_0	$\eta_b(1S)$	$9.398~{ m GeV}$	$9.398~{ m GeV}$	0.001%
$1^{3}S_{1}$	$\Upsilon(1S)$	9.461 GeV	9.461 GeV	0.004%
$1^{3}P_{0}$	$\chi_{b0}(1P)$	$9.859~{ m GeV}$		0.21%
$1^{3}P_{1}$	$\chi_{b1}(1P)$	$9.893~{ m GeV}$	9.869 GeV	
$1^{3}P_{2}$	$\chi_{b2}(1P)$	$9.912~{ m GeV}$		
$1^{1}P_{1}$	$h_b(1P)$	$9.899~{ m GeV}$		
2^1S_0	$\eta_b(2S)$	$9.999~{ m GeV}$	9.977 GeV	0.22%
2^3S_1	$\Upsilon(2S)$	$10.002~{ m GeV}$	$9.999~{ m GeV}$	0.03%
$2^{3}P_{0}$	$\chi_{b0}(2P)$	$10.232~{ m GeV}$		0.05%
$2^{3}P_{1}$	$\chi_{b1}(2P)$	$10.255~\mathrm{GeV}$	10.246 GeV	
$2^{3}P_{2}$	$\chi_{b2}(2P)$	$10.269~{ m GeV}$		
2^1P_1	$h_b(2P)$	-		
$3^{1}S_{0}$	$\eta_b(3S)$	-	$10.344~\mathrm{GeV}$	_
$3^{3}S_{1}$	$\Upsilon(3S)$	$10.355~\mathrm{GeV}$	$10.358~{ m GeV}$	0.03%

J. Alford and MS, 1309.3003

- As the table to the right shows, it works quite well
- Maximum error in the masses of the bottomonium sates is 0.22%

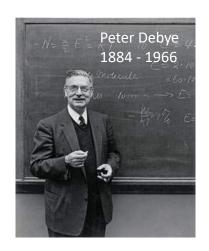


Screening of electric interaction with screening length $r_D = 1/m_D$

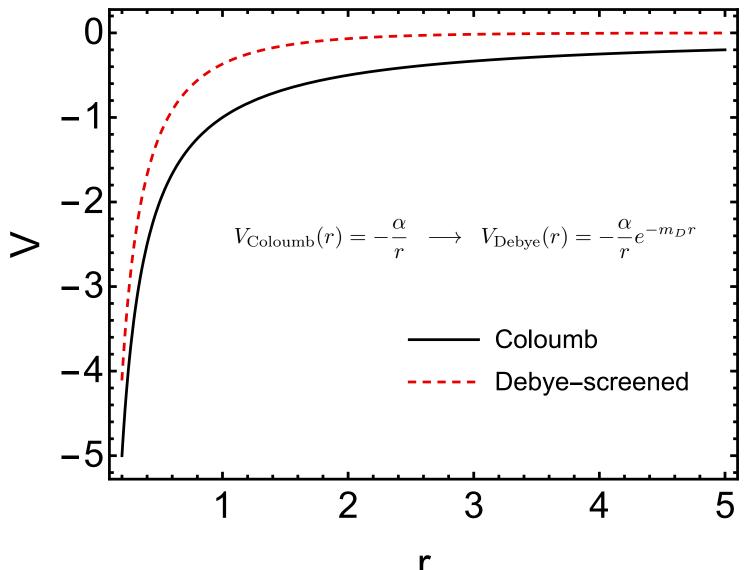


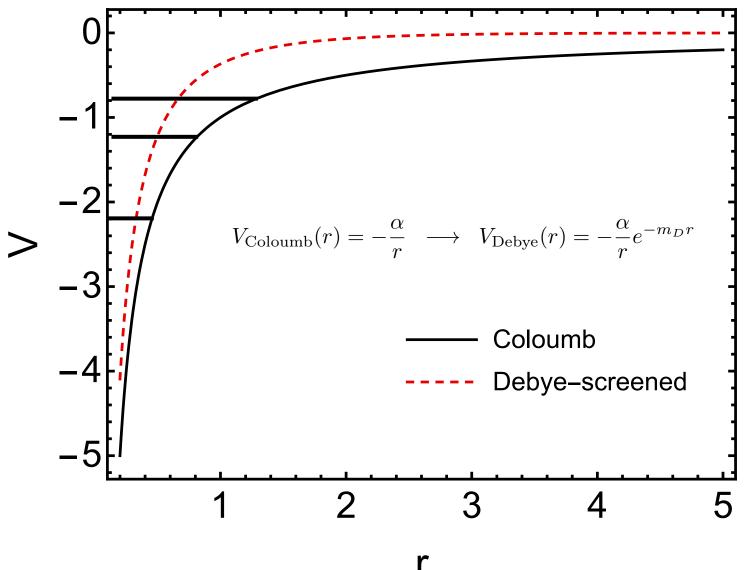
A test charge polarizes the particles of the plasma and they "screen" its charge

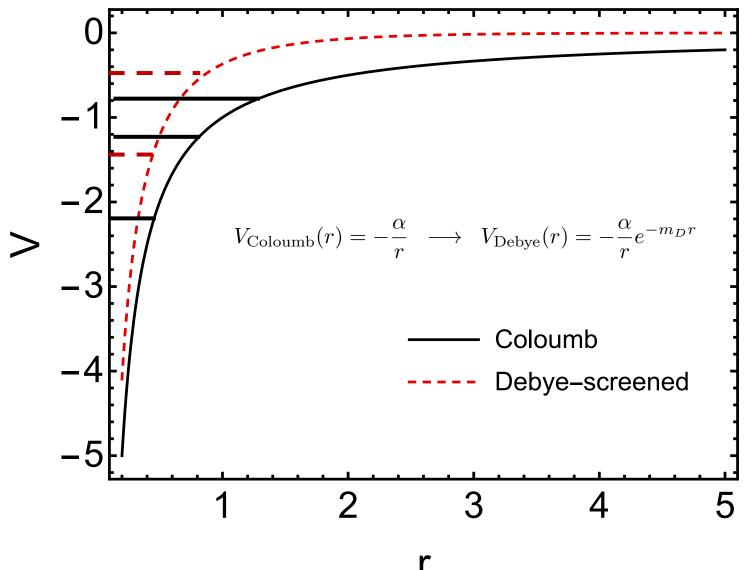
$$V_{\text{Coloumb}}(r) = -\frac{\alpha}{r} \longrightarrow V_{\text{Debye}}(r) = -\frac{\alpha}{r}e^{-m_D r}$$



- The same phenomena that occurs in an electric plasma occurs in the QGP
- A screening mass m_D ~ gT is generated by strong interactions of quarks and gluons







In-medium breakup (decay) rates

- In addition to Debye screening, which reduces the effective coupling between quarks and antiquarks, the states also acquire a temperature dependent breakup rate (width) which increases as the temperature increases.
- Primarily, heavy quark bound states breakup via strong processes which result in the quark/antiquark becoming unbound inside of the QGP, e.g. Landau damping, collisional disassociation, etc.

In-medium heavy quark potential

Using the real-time formalism one can express the potential in terms of the *static* advanced, retarded, and Feynman propagators

$$V(\mathbf{r},\xi) = -g^2 C_F \int \frac{d^3 \mathbf{p}}{(2\pi)^3} \left(e^{i\mathbf{p}\cdot\mathbf{r}} - 1 \right) \frac{1}{2} \left(D^*_R^L + D^*_A^L + D^*_F^L \right)$$

Real part can be written as

$$Re[V(\mathbf{r},\xi)] = -g^2 C_F \int \frac{d^3 \mathbf{p}}{(2\pi)^3} e^{i\mathbf{p}\cdot\mathbf{r}} \frac{\mathbf{p}^2 + m_\alpha^2 + m_\gamma^2}{(\mathbf{p}^2 + m_\alpha^2 + m_\gamma^2)(\mathbf{p}^2 + m_\beta^2) - m_\delta^4}$$

With <u>direction-dependent masses</u>, e.g.

$$m_{\alpha}^2 = -\frac{m_D^2}{2p_{\perp}^2\sqrt{\xi}} \left(p_z^2 \arctan\sqrt{\xi} - \frac{p_z\mathbf{p}^2}{\sqrt{\mathbf{p}^2 + \xi p_{\perp}^2}} \arctan\frac{\sqrt{\xi}p_z}{\sqrt{\mathbf{p}^2 + \xi p_{\perp}^2}} \right)$$

Anisotropic potential calculation: Dumitru, Guo, and MS, 0711.4722 and 0903.4703 Gluon propagator in an anisotropic plasma: Romatschke and MS, hep-ph/0304092

Complex-valued Potential

- Anisotropic potential can be parameterized as a Debye-screened potential with a direction-dependent Debye mass
- The potential also has an imaginary part coming from the Landau damping of the exchanged gluon!
- This imaginary part also exists in the isotropic case Laine et al hep-ph/0611300
- Used this as a model for the free energy (F) and also obtained internal energy (U) from this.

$$V_{\text{screened}}(r, \theta, \xi, \Lambda) = -C_F \alpha_s \frac{e^{-\mu(\theta, \xi, \Lambda)r}}{r}$$

MS, 1106.2571; Bazow and MS, 1112.2761

$$V_{
m R}({f r}) = -rac{lpha}{r}\left(1+\mu\,r
ight)\exp\left(-\mu\,r
ight) \ + rac{2\sigma}{\mu}\left[1-\exp\left(-\mu\,r
ight)
ight] \ - \sigma\,r\,\exp(-\mu\,r) - rac{0.8\,\sigma}{m_Q^2\,r}$$

Dumitru, Guo, Mocsy, and MS, 0901.1998

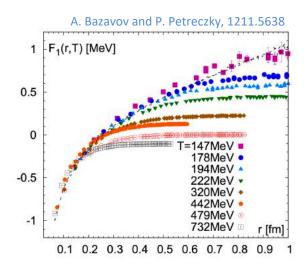
$$V_{\rm I}(\mathbf{r}) = -C_F \alpha_s p_{\rm hard} \left[\phi(\hat{r}) - \xi \left(\psi_1(\hat{r}, \theta) + \psi_2(\hat{r}, \theta) \right) \right]$$

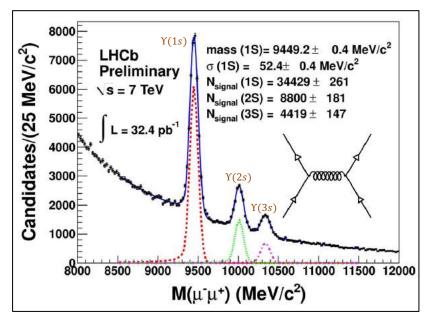
Dumitru, Guo, and MS, 0711.4722 and 0903.4703 Burnier, Laine, Vepsalainen, arXiv:0903.3467 (aniso)

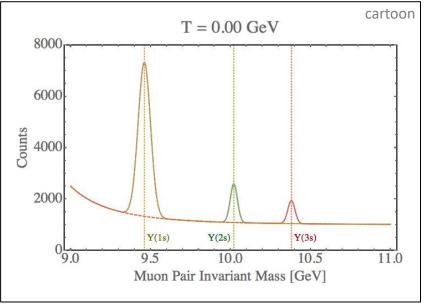
 In a high temperature quark-gluon plasma we expect weaker color binding (<u>Debye screening</u> + asymptotic freedom)

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E. V. Shuryak, Phys. Rept. 61, 71–158 (1980)
T. Matsui, and H. Satz, Phys. Lett. B178, 416 (1986)
F. Karsch, M. T. Mehr. and H. Satz, Z. Phys. C37, 617 (1988)
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 Also, high energy plasma particles which slam into the bound states cause them to have shorter lifetimes -> larger spectral widths



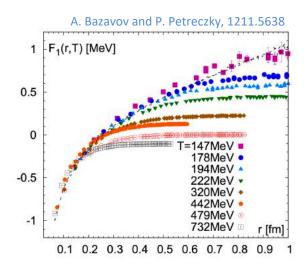


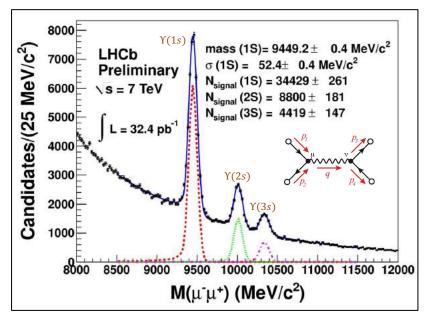


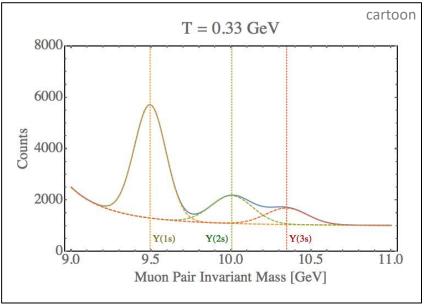
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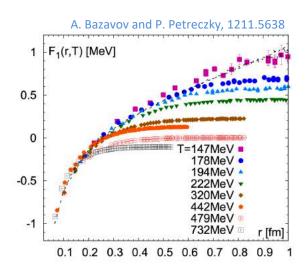


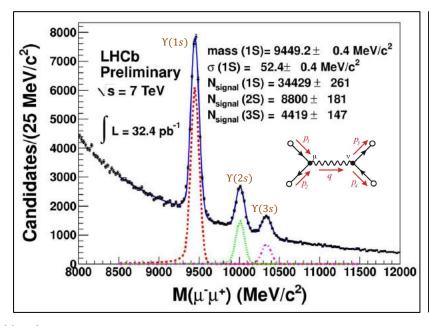


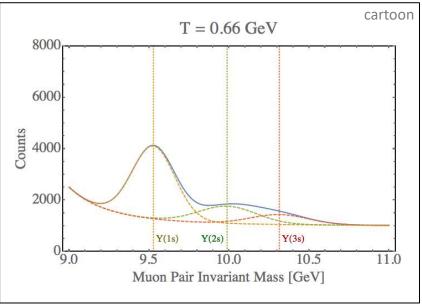
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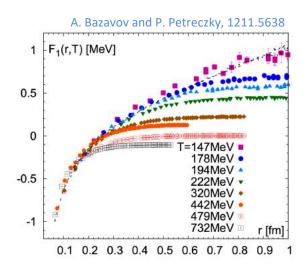


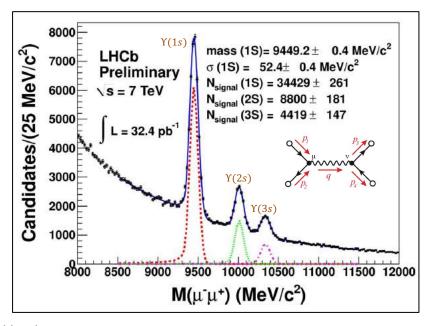


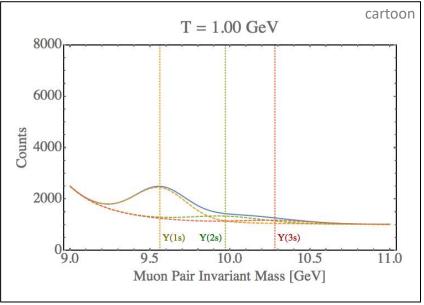
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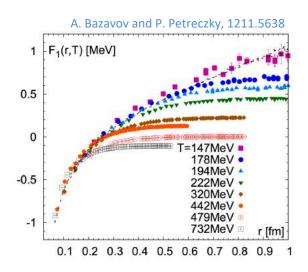


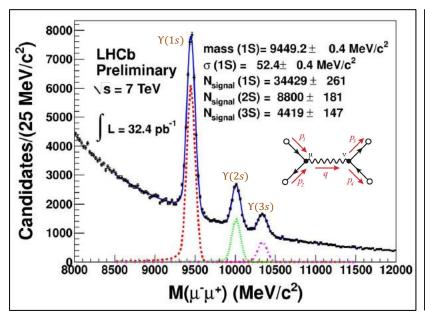


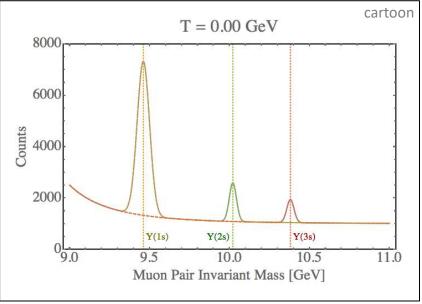
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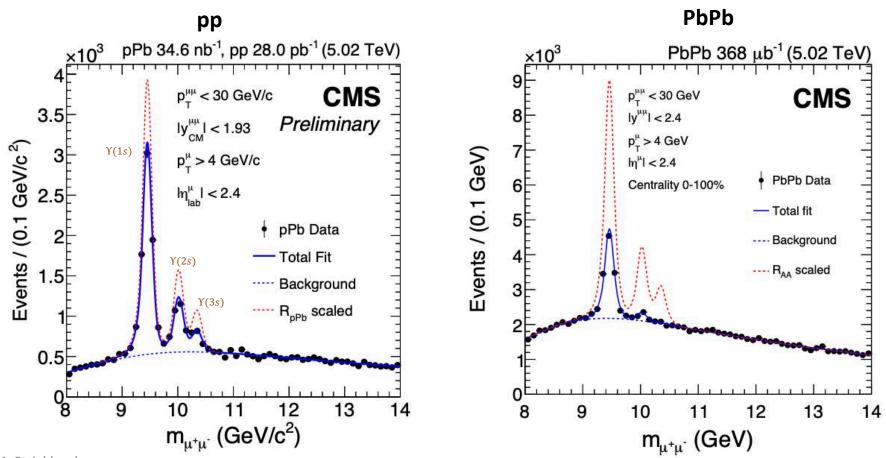




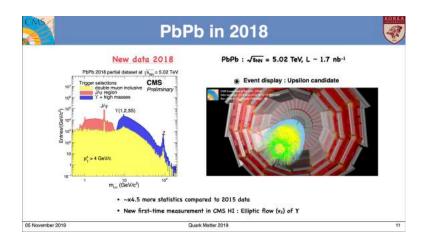


CMS 2019 Data – 5.02 TeV Dimuon Spectra

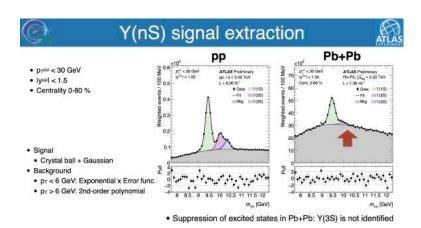
The **CMS** (Compact Muon Solenoid) experiment has measured bottomonium spectra for both pp and Pb-Pb collisions. With this we can extract R_{AA} experimentally.

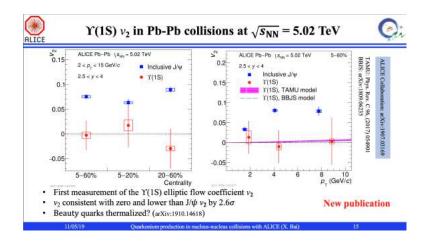


New data at QM19



- New data from CMS and ALICE
- Sufficient statistics to start extracting production anisotropies
- First data from ATLAS collaboration; data explained well by KSU in-medium breakup model
- LHCb is joining the effort (high mom res)

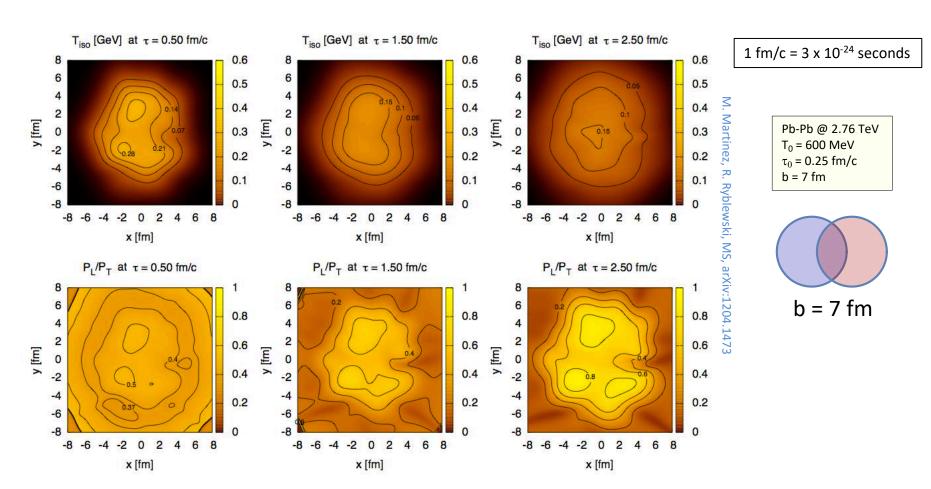




Theory

Conceptually simple calculation

For in-medium suppression, given the population of quarkonia states at some τ_0 , we can simply integrate the <u>instantaneous decay/regeneration rate</u> of the state $\Gamma(\tau, x, y, \eta)$ over the QGP spatiotemporal evolution to obtain the **survival probability**.



Summary of adiabatic the method

Solve the 3d Schrödinger EQ with a complex-valued potential

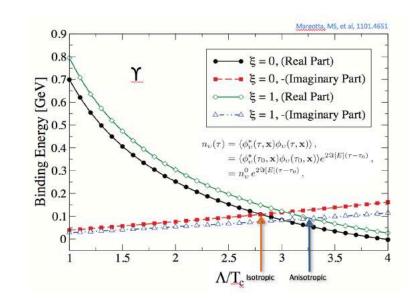


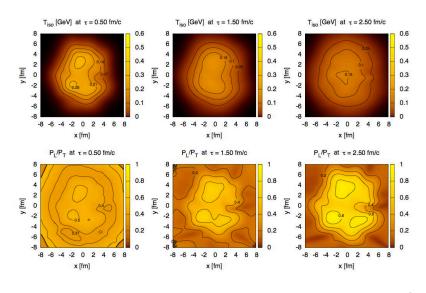
Obtain the real and imaginary parts of the binding energies for the Y(1s), Y(2s), Y(3s), χ_{b1} , and χ_{b2} as function of energy density and momentum-anisotropy.

Yager-Elorriaga and MS, 0901.1998; Margotta, MS, et al, 1101.4651



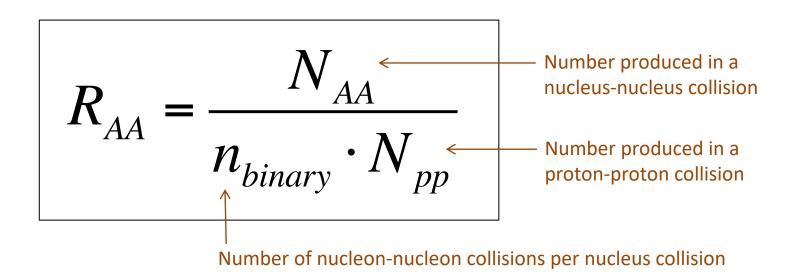
Fold together with the non-EQ spatiotemporal evolution to obtain the **survival probability**.



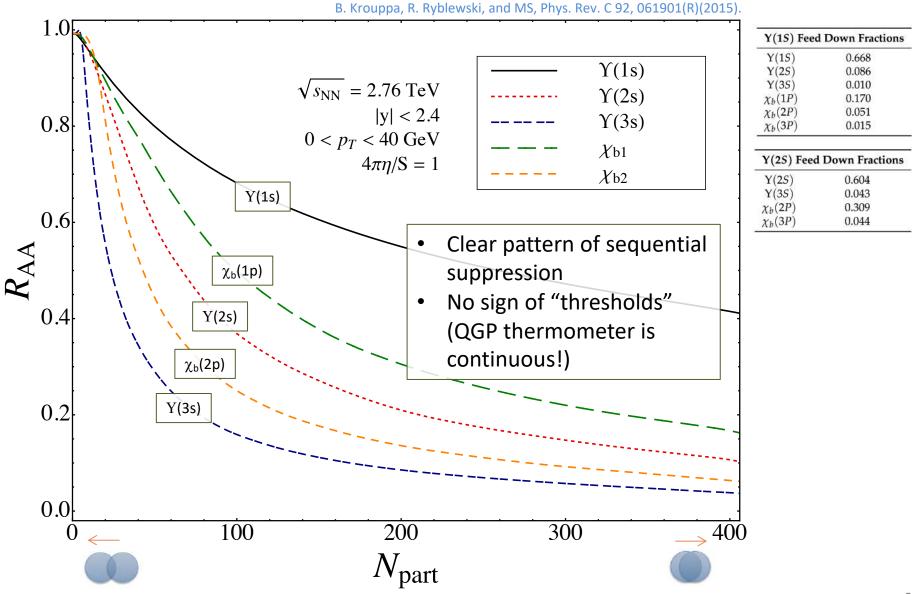


The suppression factor

• The suppression factor, \mathbf{R}_{AA} , is the ratio of the number of a particular type of particle produced in a collision of two symmetric nuclei (AA) to the amount produced in a proton-proton (pp) collision scaled by the expected number of nucleon-nucleon collisions



State Suppression Factors, $R_{AA}{}^{i}$

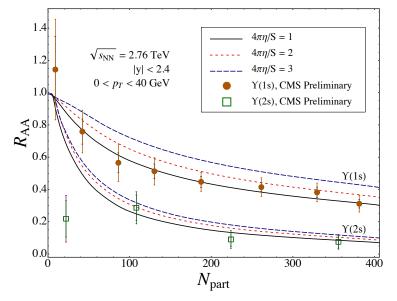


Facing the experimental data...

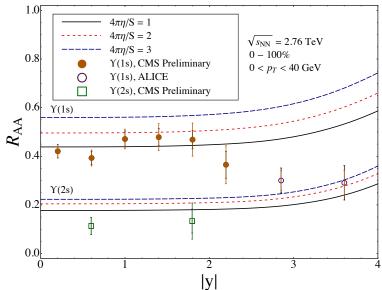
Adiabatic approximation

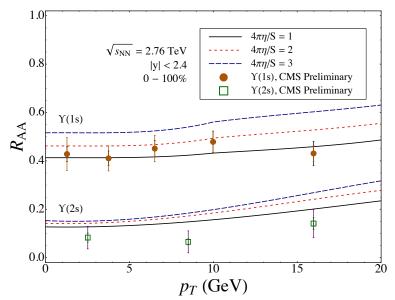
Inclusive Bottomonium Suppression @ 2.76 TeV





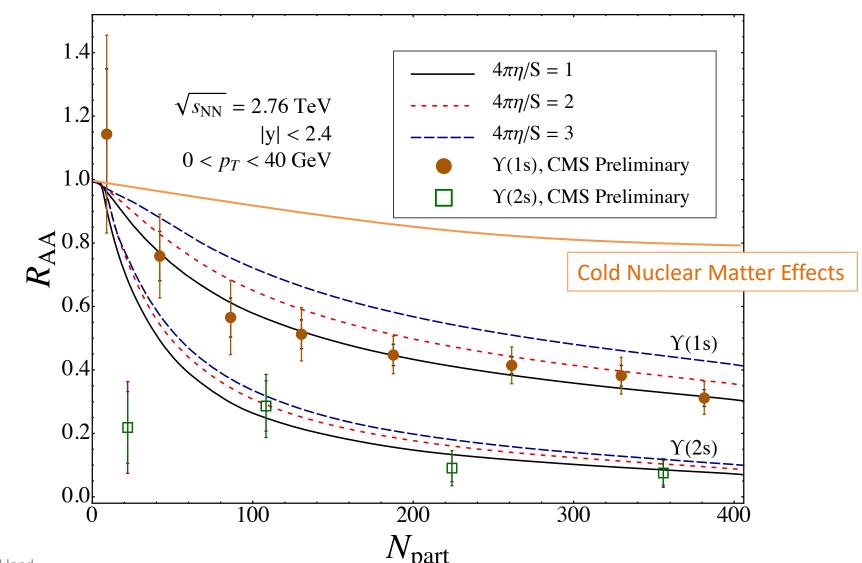
- Compare model to 2.76 TeV data from CMS and ALICE
- Reasonable agreement with CMS data but not perfect
- Disagreement with ALICE data in rapidity range 2.5 < y < 4
- Model slightly underpredicts Y(2s) suppression





Inclusive Bottomonium Suppression @ 2.76 TeV

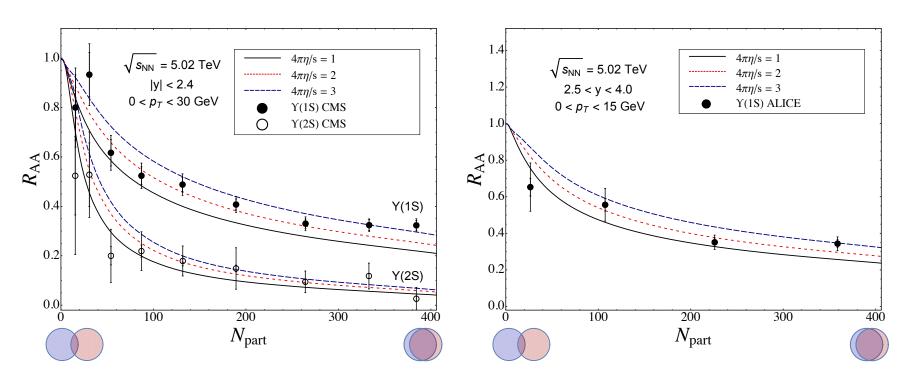
B. Krouppa, R. Ryblewski, and MS, Phys. Rev. C 92, 061901(R) (2015).



Inclusive Bottomonium Suppression @ 5.02 TeV

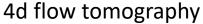
B. Krouppa, R. Ryblewski, and MS 1704.02361

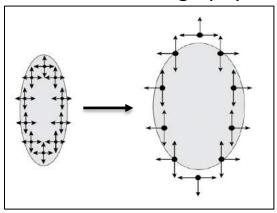
- Model predictions compared to CMS data (left) and ALICE data (right)
- Results below are as a function of N_{part}

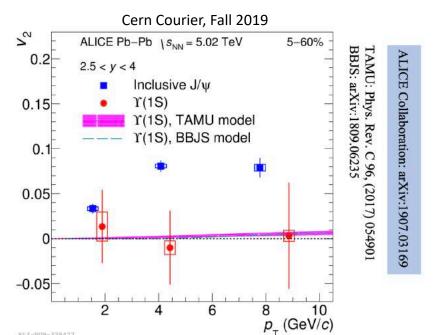


• CMS (left) covers central rapidity (|y| < 2.4) and ALICE (right) covers forward rapidity (2.5 < |y| < 4)

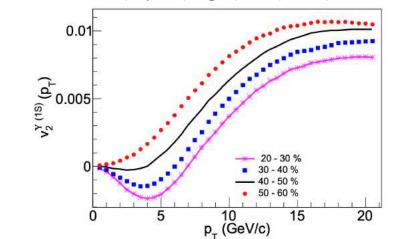
Bottomonium "flow" ... or lack thereof

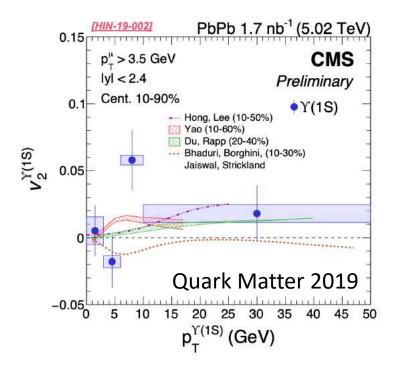






Bhadhuri, Algahtani, Borghini, Jaiswal, and MS, 2007.03939





M. Strickland

ALI-PUB-325477

Facing the experimental data...

Real-time quantum evolution

NEW: Heavy Quarkonium Quantum Dynamics (HQQD) A. Islam and MS, forthcoming.

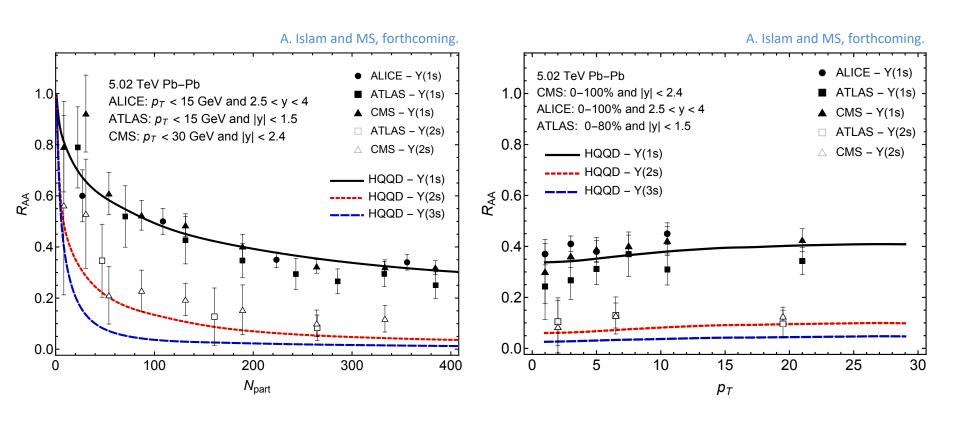
- Sample bottomonium production points from binary collision overlap profile
- Sample bottomonium initial momentum using pp experimental results
- Calculate suppression for each of the states under consideration (1s, 2s, 3p, 3s, 3p) by solving 3D Schrödinger equation numerically for each trajectory.
- Compute total number of produced states of each type
- Then, take into account late-time feed down using a feed-down matrix constructed from PDG branching

$$\vec{N}_{\mathrm{final}} = F \vec{N}_{\mathrm{QGP}} \qquad F = \begin{pmatrix} 1 & 0.265 & 0.184 & 0.0657 & 0.0650 \\ 0 & 0.735 & 0 & 0.1060 & 0.0946 \\ 0 & 0 & 0.816 & 0 & 0.0047 \\ 0 & 0 & 0 & 0.8283 & 0 \\ 0 & 0 & 0 & 0 & 0.8357 \end{pmatrix}$$

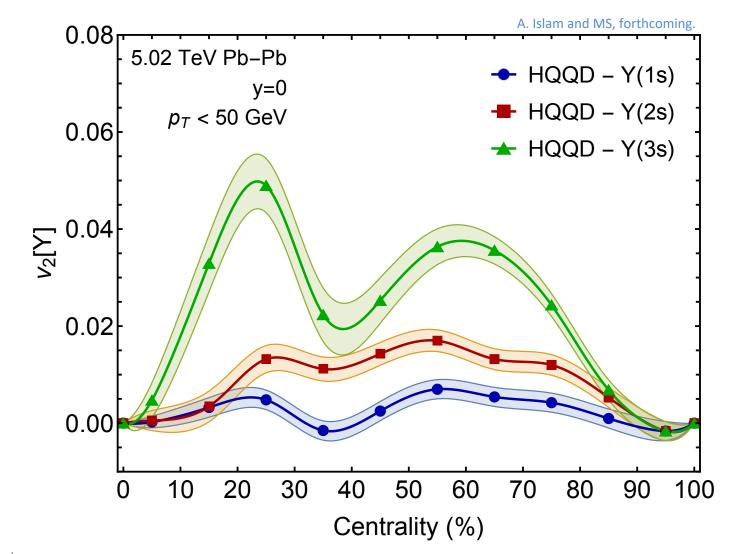
- To obtain RAA, we then divide by the Nbin-scaled pp-production cross sections.
- To obtain vn, we compute <cos(nf)>
- Errors reported are statistical

 1.2 million sampled trajectories

HQQD RAA vs experimental data

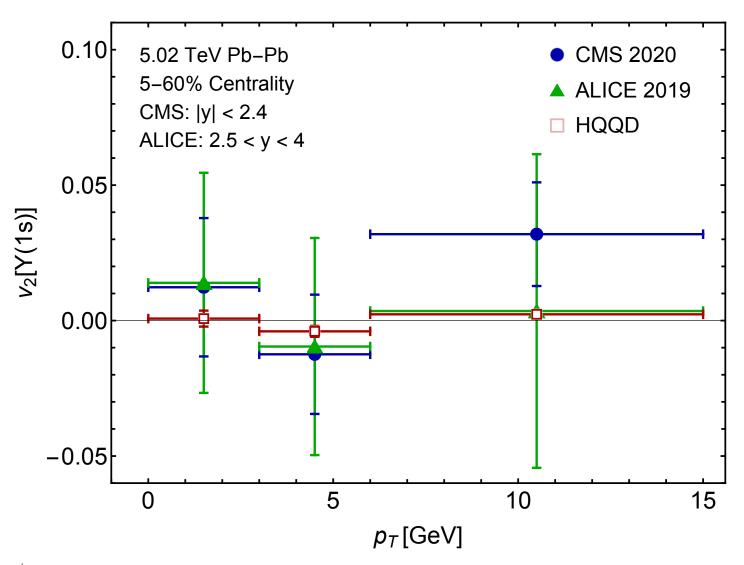


HQQD v2 predictions



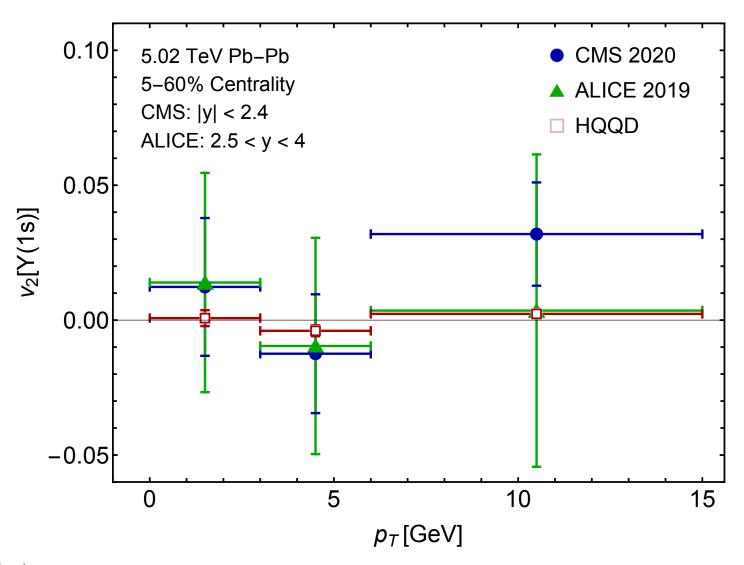
HQQD comparison to data

A. Islam and MS, forthcoming.

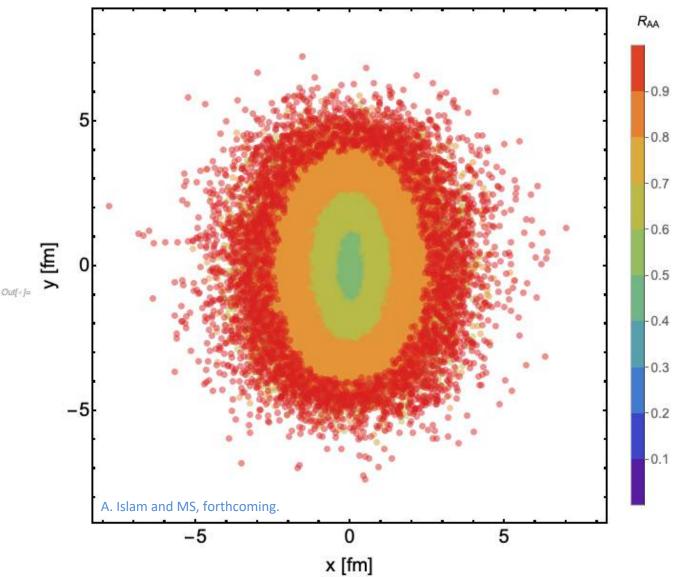


HQQD comparison to data

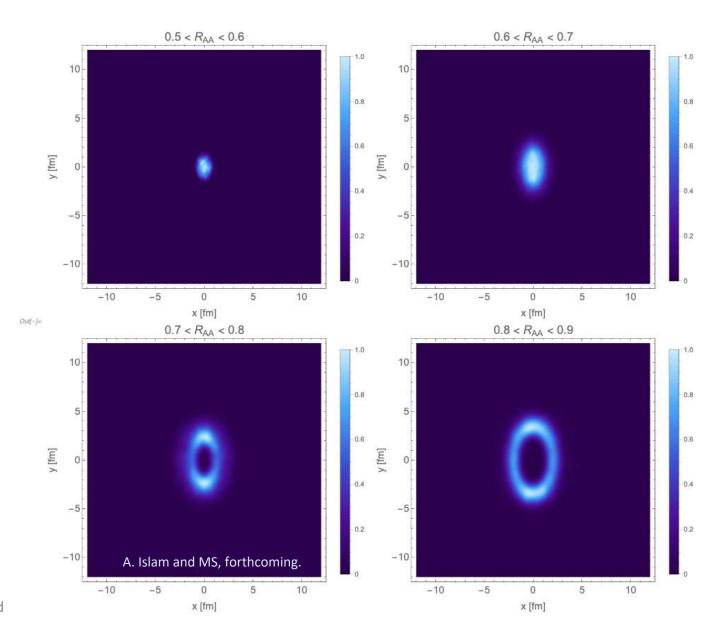
A. Islam and MS, forthcoming.



QGP tomography



QGP tomography



Conclusions and Outlook

- The suppression of bottomonium is a smoking gun for the creation of the QGP
- Initial state effects (aka cold nuclear matter effects) are not enough to explain the experimental observations.
- Complex screening model works reasonably well to describe the suppression seen at LHC → QGP!
- There is much work to do on this problem. One thing I did not discuss today was "regeneration". This occurs when the density of heavy (anti-)quarks becomes large, making it probable for a pair to recombine in the QGP. At very high temperatures/beam energies this effect is important for charm quarks, but still not so important for bottom quarks.
- Showed forthcoming work on improving calculations to include full real-time in-medium Schrödinger equation evolution (student A. Islam) → in-medium quantum regeneration